

**ICS 202 — Data Structures and Algorithms**  
**ICS Department, KFUPM**

Term 211

Quiz 4 [V3]

Student ID: \_\_\_\_\_ Name: \_\_\_\_\_ Section: \_\_\_\_\_

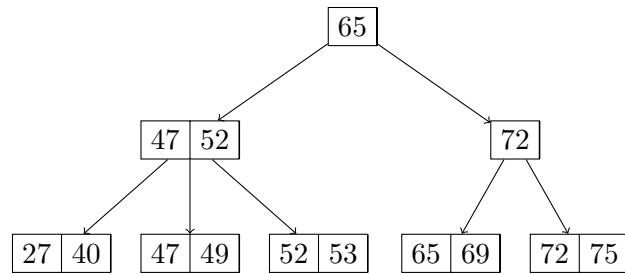
1. [5 marks] Insert the following keys sequentially in an empty B tree [m = 5]: 35, 49, 46, 47, 51, 33, 34, 45.

Draw the tree after each key insertion and mention if any operation (merging/rotation/split) is required.

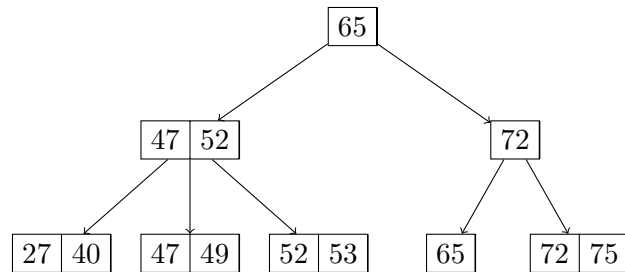
<p>Step 1[if needed]</p> <div style="text-align: center; margin: 20px 0;"> <div style="border: 1px solid black; width: 30px; height: 20px; margin: 0 auto; display: flex; align-items: center; justify-content: center;">35</div> <p>Inserting 35</p> </div>	<p>Step 2[if needed]</p> <div style="text-align: center; margin: 20px 0;"> <div style="border: 1px solid black; width: 60px; height: 20px; margin: 0 auto; display: flex; align-items: center; justify-content: space-around;">35 49</div> <p>Inserting 49</p> </div>	<p>Step 3[if needed]</p> <div style="text-align: center; margin: 20px 0;"> <div style="border: 1px solid black; width: 90px; height: 20px; margin: 0 auto; display: flex; align-items: center; justify-content: space-around;">35 46 49</div> <p>Inserting 46</p> </div>
<p>Step 4[if needed]</p> <div style="text-align: center; margin: 20px 0;"> <div style="border: 1px solid black; width: 120px; height: 20px; margin: 0 auto; display: flex; align-items: center; justify-content: space-around;">35 46 47 49</div> <p>Inserting 47</p> </div>	<p>Step 5[if needed]</p> <div style="text-align: center; margin: 20px 0;"> <div style="margin-bottom: 10px;"> <div style="border: 1px solid black; width: 30px; height: 20px; margin: 0 auto; display: flex; align-items: center; justify-content: center;">47</div> <div style="display: flex; justify-content: space-around; width: 100%;"> <div style="border: 1px solid black; width: 40px; height: 20px; display: flex; align-items: center; justify-content: center;">35 46</div> <div style="border: 1px solid black; width: 40px; height: 20px; display: flex; align-items: center; justify-content: center;">49 51</div> </div> </div> <p>Inserting 51 and Split</p> </div>	<p>Step 6[if needed]</p> <div style="text-align: center; margin: 20px 0;"> <div style="margin-bottom: 10px;"> <div style="border: 1px solid black; width: 30px; height: 20px; margin: 0 auto; display: flex; align-items: center; justify-content: center;">47</div> <div style="display: flex; justify-content: space-around; width: 100%;"> <div style="border: 1px solid black; width: 60px; height: 20px; display: flex; align-items: center; justify-content: center;">33 35 46</div> <div style="border: 1px solid black; width: 40px; height: 20px; display: flex; align-items: center; justify-content: center;">49 51</div> </div> </div> <p>Inserting 33</p> </div>
<p>Step 7[if needed]</p> <div style="text-align: center; margin: 20px 0;"> <div style="margin-bottom: 10px;"> <div style="border: 1px solid black; width: 30px; height: 20px; margin: 0 auto; display: flex; align-items: center; justify-content: center;">47</div> <div style="display: flex; justify-content: space-around; width: 100%;"> <div style="border: 1px solid black; width: 100px; height: 20px; display: flex; align-items: center; justify-content: center;">33 34 35 46</div> <div style="border: 1px solid black; width: 40px; height: 20px; display: flex; align-items: center; justify-content: center;">49 51</div> </div> </div> <p>Inserting 34</p> </div>	<p>Step 8[if needed]</p> <div style="text-align: center; margin: 20px 0;"> <div style="margin-bottom: 10px;"> <div style="border: 1px solid black; width: 60px; height: 20px; margin: 0 auto; display: flex; align-items: center; justify-content: space-around;">35 47</div> <div style="display: flex; justify-content: space-around; width: 100%;"> <div style="border: 1px solid black; width: 40px; height: 20px; display: flex; align-items: center; justify-content: center;">33 34</div> <div style="border: 1px solid black; width: 40px; height: 20px; display: flex; align-items: center; justify-content: center;">45 46</div> <div style="border: 1px solid black; width: 40px; height: 20px; display: flex; align-items: center; justify-content: center;">49 51</div> </div> </div> <p>Inserting 45 and Split</p> </div>	<p>Step 9[if needed]</p>

## ICS 202 — Data Structures and Algorithms

2. [5 marks] Draw the tree at each step and mention each type of operation (merging/rotation/split) when the key 69 is deleted from the following B+ tree of order  $M = 4$  and  $L = 4$ .

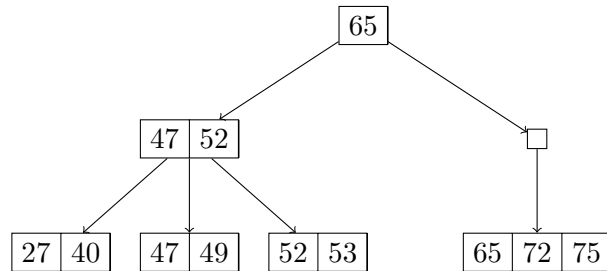


Step 1 [if needed]



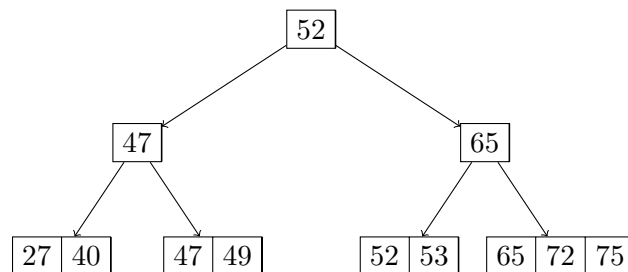
Underflow at 65

Step 2 [if needed]



Merging but Underflow Again

Step 3 [if needed]



Right Rotation from Left branch