King Fahd University of Petroleum and Minerals

College of Computer Science and Engineering Information and Computer Science Department

ICS 353-01: Design and Analysis of Algorithms Fall Semester 2018-2019 Quiz#2, Sunday September 30th, 2018.

Name:

ID#:

1. (10 points) Express the function $f(n) = n^2 \log n + \frac{n^3 + 5}{n + 2}$ in terms of Big $\Theta()$ notation. Prove your answer.

$$\frac{n^{2}-2n+4}{n+2} = n^{2}-2n+4 - \frac{3}{n+2}, \text{ which is } \oplus \omega$$

$$\lim_{n\to\infty} n^{2} \int_{n}^{n} \int_{n}^{n} \int_{n\to\infty}^{n} \int_{n\to\infty}^{n} \int_{n}^{n} \int_{n}^{n$$

$$\sum_{i=1}^{n} i = \frac{n(n+1)}{2} \qquad \sum_{i=1}^{n} i^{2} = \frac{n(n+1)(2n+1)}{6} \qquad \sum_{i=1}^{n} i^{3} = \left(\frac{n(n+1)}{2}\right)^{2}$$

$$\sum_{i=0}^{n} x^{i} = \frac{x^{n+1}-1}{x-1} \qquad \sum_{i=1}^{n} \left(\frac{1}{2}\right)^{i} \cdot i = 2 - \frac{n+2}{2^{n}} \qquad 2^{\lg n} = n$$

$$\log_{b} a = \frac{\log_{c} a}{\log_{a} b} \text{ where } c, b \neq 1 \qquad \log_{a} b = \log_{a} a + \log_{a} b$$

- 2. (10 points) Consider the following algorithm:
 - 1. Sum := 0;
 - 2. for j := 1 to n^2 do
 - 3. i = 1;
 - 4. while $(i \le n)$ do
 - $5. ext{sum} := ext{sum} + 1;$
 - 6. i := i * 2;
 - 7. end while;
 - 8. end for;
 - 9. return sum;
 - a. (4 points) Express the number of times step 5 gets executed in summation form.
 - b. (4 points) Evaluate the summation of part (a).
 - c. (2 points) Express the time complexity of the algorithm using Big Θ () notation.